

Interpret R output in Holt Winters function

Simple Exponential

$$= \beta_0 + \epsilon_t \leftarrow \begin{matrix} \text{wh. noise} \\ \uparrow \\ \text{mean/level} \end{matrix}$$

Smoothing Equation

$$l_t = \hat{y}_t = \alpha y_{t-1} + (1-\alpha) l_{t-1}; 0 < \alpha < 1.$$

\uparrow
smoothing filter.

R output language

estimate of β_0 is $\hat{\beta}_0 = a$
(in R)
 $\alpha = \text{alpha (in R)}$

Holt Exponential Smoothing.

$$= \beta_0 + \beta_1 t + \epsilon_t.$$

\uparrow mean/level \nwarrow Growth (trend rate)

$$l_t = \hat{y}_t = \alpha y_t + (1-\alpha) (l_{t-1} + b_{t-1}) \rightarrow \text{Smoothing eqn for level}$$

$$b_t = \gamma (l_t - l_{t-1}) + (1-\gamma) b_{t-1} \rightarrow \text{smoothing eqn for trend}$$

Smoothing filters α, γ .

$\hat{\beta}_0 = a$ (in R)
 $\hat{\beta}_1 = b$ (in R)
 $\alpha = \text{alpha (in R)}$
 $\gamma = \text{beta (in R)}$

Holt Winters potential method

$$= (\beta_0 + \beta_1 t) S_{nt} \times \epsilon_t \quad (\text{IR})$$

Multiplicative

$$= (\beta_0 + \beta_1 t) + S_{nt} + \epsilon_t$$

Additive.

$$l_t = \alpha (y_t / S_{nt-l}) + (1-\alpha) (l_{t-1} + b_{t-1})$$

$$b_t = \gamma (l_t - l_{t-1}) + (1-\gamma) b_{t-1}$$

$$S_{nt} = \delta (y_t / l_t) + (1-\delta) S_{nt-l}$$

$l = \text{no of seasons in a year}$
For monthly $l=12$, for quarterly $l=4$

$\hat{\beta}_0 = a$ (in R)
 $\hat{\beta}_1 = b$ (in R)
 $S_1, S_2, \dots, S_{12} = \text{seasonal effect estimation (monthly data)}$
 $\alpha = \text{alpha (in R)}$
 $\gamma = \text{beta (in R)}$
 $\delta = \text{delta (in R)}$